## Trigonometry

## Instructional Focus: Use unit circles and inverse trigonometric functions

	4 – Mastery	3 – Proficient	2 - Basic	1 – Below Basic	0 – No
					Evidence
Use special	Can extend	Use special triangles to	Use special triangles to	Use special triangles to	Little
triangles	thinking beyond	determine the values of	determine the values of	determine the values of	evidence
(F.TF.3)	the standard,	sine, cosine, tangent,	sine, cosine, tangent,	sine, cosine and tangent for	of
	including tasks	secant, cosecant, and	secant, cosecant, and	$\pi/6$ , $\pi/4$ and $\pi/3$	reasoning
	that may involve	cotangent for 0, $\pi/6$ , $\pi/4$	<u>cotangent</u> for <b>0</b> , $\pi/6$ , $\pi/4$ ,		or
	one of the	and π/3, π/2 and <u>use the</u> unit circle to express the	π/3 and <u>π/2</u>		application
	following:	values of sine, cosine,			to solve
		tangent, secant, cosecant,			the
		and cotangent for $\pi - x$ , $\pi + x$ ,			problem
	Designing	and $2\pi - x$ in terms of their			problem
	Connecting	values for x, where x is any			
	<ul> <li>Synthesizing</li> </ul>	<u>real number</u>			Descent
Use unit	<ul> <li>Applying</li> </ul>	Use the unit circle to	Use the unit circle to	Use the unit circle to	Does not
circles to	<ul> <li>Justifying</li> </ul>	express any angle, including	express any angle, between	express any angle, between	meet the
find values	Critiquing	negative angles and angles	0 and $2\pi$ , in terms of its	0 and $2\pi$ , in terms of its	criteria in
(F.TF.4)	<ul> <li>Analyzing</li> </ul>	involving more than 1	standard position to find	standard position to find	a level 1
	Creating	rotation, in terms of its	ALL 6 trig functions.	the sine, cosine, and	
	<ul> <li>Proving</li> </ul>	standard position to find <u>all</u>		tangent functions.	
Construct		six trigonometric functions. Construct an invertible	Identify a domain that will	Given a portion of a	
Inverse		trigonometric function by	allow construction of the	trigonometric graph,	
		restricting the domain so	inverse of a trigonometric	identify if that part of the	
trigono-		that the function is always	function, because the	graph is invertible	
metric		increasing or decreasing	function would be always		
functions			increasing or decreasing		
(F.TF.6)					
Use inverse		Use inverse functions to	Use inverse functions to	Use inverse functions to	
trigono-		solve trigonometric	solve trigonometric	solve trigonometric	
metric		equations with restricted	equations with restricted	equations with restricted	
functions		and unrestricted domains	and unrestricted domains	<u>domains</u>	
(F.TF.7)		and interpret the solutions			
		in context of the situation			
Pythagor-		<u><b>Prove</b></u> the Pythagorean	Use the Pythagorean identity $sin^2(\theta) + cos^2(\theta) =$	Use the Pythagorean identity $sin^2(\theta) + cos^2(\theta) =$	
ean		identity $sin^2(\theta) + cos^2(\theta) =$ 1 and use it to find $sin(\theta)$ ,	identity $sin^2(\theta) + cos^2(\theta) =$ 1 to find $sin(\theta), cos(\theta),$	identity $sin^{2}(\theta) + cos^{2}(\theta) =$ 1 to find $sin(\theta), cos(\theta), or$	
identity		$\cos(\theta)$ , and $\tan(\theta)$	$\underline{and} tan(\theta)$	$tan(\theta)$	
(F.TF.8)					
Given $\cos \theta = \frac{1}{2}$					
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F.TF.3 (+) Use special triangles to determine geometrically the values of sine, cosine, tangent for  $\pi/3$ ,  $\pi/4$  and  $\pi/6$ , and use the unit circle to express the values of sine, cosine, and tangent for  $\pi-x$ ,  $\pi+x$ , and  $2\pi-x$  in terms of their values for x, where x is any real number. Functions F.TF.4 (+) Use the unit circle to explain symmetry (odd and even) and periodicity of trigonometric functions.

F.TF.6 (+) Understand that restricting a trigonometric function to a domain on which it is always increasing or always decreasing allows its inverse to be constructed.

F.TF.7 (+) Use inverse functions to solve trigonometric equations that arise in modeling contexts; evaluate the solutions using technology, and interpret them in terms of the context.  $\star$ 

F.TF.8 Prove the Pythagorean identity  $sin^{2}(\theta) + cos^{2}(\theta) = 1$  and use it to find  $sin(\theta)$ ,  $cos(\theta)$ , or  $tan(\theta)$  given  $sin(\theta)$ ,  $cos(\theta)$ , or  $tan(\theta)$  and the quadrant of the angle.